

Synchronised firing patterns in a random network of adaptive exponential integrate-and-fire neuron model



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ARTICLE INFO

Article history:

Received 15 July 2016

Received in revised form 26 February 2017

Accepted 9 March 2017

Available online 16 March 2017

Keywords:

Synchronisation
Integrate-and-fire
Network

ABSTRACT

We have studied neuronal synchronisation in a random network of adaptive exponential integrate-and-fire neurons. We study how spiking or bursting synchronous behaviour appears as a function of the coupling strength and the probability of connections, by constructing parameter spaces that identify these synchronous behaviours from measurements of the inter-spike interval and the calculation of the order parameter. Moreover, we verify the robustness of synchronisation by applying an external perturbation to each neuron. The simulations show that bursting synchronisation is more robust than spike synchronisation.

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1. Introduction

The concept of synchronisation is based on the adjustment of rhythms of oscillating systems due to their interaction (Pikovsky, Rosenblum, & Kurths, 2001). Synchronisation phenomenon was recognised by Huygens in the 17th century, time when he performed experiments to understand this phenomenon (Bennet, Schatz, Rockwood, & Wiesenfeld, 2002). To date, several kinds of synchronisation among coupled systems were reported, such as complete (Li & Li, 2016), phase (Batista, Lopes, Viana, & Batista, 2010; Pereira, Baptista, & Kurths, 2007), lag (Huang, Li, Huang, & He, 2014), and collective almost synchronisation (Baptista et al., 2012).

Neuronal synchronous rhythms have been observed in a wide range of researches about cognitive functions (Hutcheon & Yarom, 2000; Wang, 2010). Electroencephalography and magnetoencephalography studies have been suggested that neuronal synchronisation in the gamma frequency plays a functional role for memories in humans (Axmacher, Mormann, Fernández, Elger, & Fell, 2006; Fell & Axmacher, 2011). Steinmetz et al. (2000) investigated the synchronous behaviour of pairs of neurons in the

secondary somatosensory cortex of monkey. They found that attention modulates oscillatory neuronal synchronisation in the somatosensory cortex. Moreover, in the literature it has been proposed that there is a relationship between conscious perception and synchronisation of neuronal activity (Hipp, Engel, & Siegel, 2011).

We study spiking and bursting synchronisation between neuron in a neuronal network model. A spike refers to the action potential generated by a neuron that rapidly rises and falls (de Lange & Hasler, 2008), while bursting refers to a sequence of spikes that are followed by a quiescent time (Wu, Lu, Lin, Leng, & Feng, 2012). It was demonstrated that spiking synchronisation is relevant to olfactory bulb (Davison, Feng, & Brown, 2001) and is involved in motor cortical functions (Riehle, Grün, Diesmann, & Aertsen, 1997). The characteristics and mechanisms of bursting synchronisation were studied in cultured cortical neurons by means of planar electrode array (Maeda, Robinson, & Kawana, 1995). Jefferys and Haas (1982) discovered synchronised bursting of CA1 hippocampal pyramidal cells.

There is a wide range of mathematical models used to describe neuronal activity, such as the cellular automaton (Viana et al., 2014), the Rulkov map (Rulkov, 2001), and differential equations (Hindmarsh & Rose, 1984; Hodgkin & Huxley, 1952). One of the simplest mathematical models and that is widely used to depict neuronal behaviour is the integrate-and-fire (Lapicque, 1907), which is governed by a linear differential equation. A more realistic

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<http://dx.doi.org/10.1016/j.neunet.2017.03.005>

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version of it is the adaptive exponential integrate-and-fire (aEIF) model which we consider in this work as the local neuronal activity of neurons in the network. The aEIF is a two-dimensional integrate-and-fire model introduced by [Brette and Gerstner \(2005\)](#). This model has an exponential spike mechanism with an adaptation current. [Touboul and Brette \(2008\)](#) studied the bifurcation diagram of the aEIF. They showed the existence of the Andronov–Hopf bifurcation and saddle–node bifurcations. The aEIF model can generate multiple firing patterns depending on the parameter and which fit experimental data from cortical neurons under current stimulation ([Naud, Marcille, Clopath, & Gerstner, 2008](#)).

In this work, we focus on the synchronisation phenomenon in a randomly connected network. This kind of network, also called Erdős–Rényi network ([Erdős & Rényi, 1959](#)), has nodes where each pair is connected according to a probability. The random neuronal network was utilised to study oscillations in cortico-thalamic circuits ([Gelenbe & Cramer, 1998](#)) and dynamics of network with synaptic depression ([Senn et al., 1996](#)). We built a random neuronal network with unidirectional connections that represent chemical synapses.

We show that there are clearly separated ranges of parameters that lead to spiking or bursting synchronisation. In addition, we analyse the robustness to external perturbation of the synchronisation. We verify that bursting synchronisation is more robustness than spiking synchronisation. However, bursting synchronisation requires larger chemical synaptic strengths, and larger voltage potential relaxation reset to appear than those required for spiking synchronisation.

This paper is organised as follows: in Section 2 we present the adaptive exponential integrate-and-fire model. In Section 3, we introduce the neuronal network with random features. In Section 4, we analyse the behaviour of spiking and bursting synchronisation. In Section 5 we draw our conclusions.

2. Adaptive exponential integrate-and-fire

As a local dynamics of the neuronal network, we consider the adaptive exponential integrate-and-fire (aEIF) model that consists of a system of two differential equations ([Brette & Gerstner, 2005](#)) given by

$$\begin{aligned} C \frac{dV}{dt} &= -g_L(V - E_L) + g_L \Delta_T \exp\left(\frac{V - V_T}{\Delta_T}\right) + I - w, \\ \tau_w \frac{dw}{dt} &= a(V - E_L) - w, \end{aligned} \quad (1)$$

where $V(t)$ is the membrane potential when a current $I(t)$ is injected, C is the membrane capacitance, g_L is the leak conductance, E_L is the resting potential, Δ_T is the slope factor, V_T is the threshold potential, w is an adaptation variable, τ_w is the time constant, and a is the level of subthreshold adaptation. The parameter Δ_T controls the sharpness of the initial phase of the spike ([Badel et al., 2008](#)) and in the limit $\Delta_T \rightarrow 0$ the neuron model becomes a standard leaky integrate-and-fire neuron model ([Clopath, Jolivet, Rauch, Lüscher, & Gerstner, 2007](#)). If $V(t)$ reaches the threshold V_{peak} , a reset condition is applied: $V \rightarrow V_r$ and $w \rightarrow w_r = w + b$. In our simulations, we consider $C = 200.0$ pF, $g_L = 12.0$ nS, $E_L = -70.0$ mV, $\Delta_T = 2.0$ mV, $V_T = -50.0$ mV, $I = 509.7$ pA, $\tau_w = 300.0$ ms, $a = 2.0$ nS, and $V_{\text{peak}} = 20.0$ mV ([Naud et al., 2008](#)).

The firing pattern depends on the reset parameters V_r and b . [Table 1](#) exhibits some values that generate five different firing patterns ([Fig. 1](#)). In [Fig. 1](#) we represent each firing pattern with a different colour in the parameter space $b \times V_r$: adaptation in red, tonic spiking in blue, initial bursting in green, regular bursting in yellow, and irregular in black. In [Fig. 1\(a\)](#), (b), and

Table 1

Reset parameters.				
Firing patterns	Fig.	b (pA)	V_r (mV)	Layout
Adaptation	1(a)	60.0	−68.0	Red
Tonic spiking	1(b)	5.0	−65.0	Blue
Initial burst	1(c)	35.0	−48.8	Green
Regular bursting	1(d)	40.0	−45.0	Yellow
Irregular	1(e)	41.2	−47.4	Black

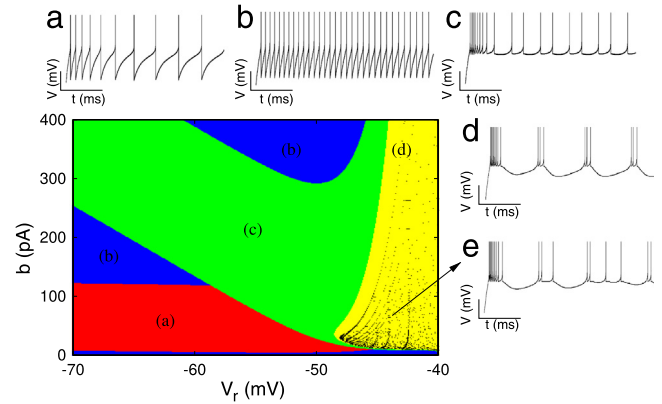


Fig. 1. (Colour online) Parameter space for the firing patterns as a function of the reset parameters V_r and b . (a) Adaptation in red, (b) tonic spiking in blue, (c) initial bursting in green, (d) regular bursting in yellow, and (e) irregular in black.

(c) we observe adaptation, tonic spiking, and initial burst pattern, respectively, due to a step current stimulation. Adaptation pattern has increasing inter-spike interval during a sustained stimulus, tonic spiking pattern is the simplest regular discharge of the action potential, and the initial bursting pattern starts with a group of spikes presenting a frequency larger than the steady state frequency. The membrane potential evolution with regular bursting is showed in [Fig. 1\(d\)](#), while [Fig. 1\(e\)](#) displays irregular pattern.

As we have interest in spiking and bursting synchronisation, we separate the parameter space into a region with spike and another with bursting patterns ([Fig. 2](#)). To identify these two regions of interest, we use the coefficient of variation (CV) of the neuronal inter-spike interval (ISI), that is given by

$$CV = \frac{\sigma_{\text{ISI}}}{\text{ISI}}, \quad (2)$$

where σ_{ISI} is the standard deviation of the ISI normalised by the mean ISI ([Gabbiani & Koch, 1998](#)). Spiking patterns produce $CV < 0.5$. Parameter regions that represent the neurons firing with spiking pattern are denoted by grey colour in [Fig. 2](#). Whereas, the black region represents the bursting patterns, which results in $CV \geq 0.5$.

3. Spiking or bursting synchronisation

In this work, we constructed a network where the neurons are randomly connected ([Erdős & Rényi, 1959](#)). Our network is given by

$$\begin{aligned} C \frac{dV_i}{dt} &= -g_L(V_i - E_L) + g_L \Delta_T \exp\left(\frac{V_i - V_T}{\Delta_T}\right) \\ &\quad + I_i - w_i + g_s(V_{\text{REV}} - V_i) \sum_{j=1}^N A_{ij} S_j + \Gamma_i, \\ \tau_w \frac{dw_i}{dt} &= a_i(V_i - E_L) - w_i, \\ \tau_s \frac{ds_i}{dt} &= -s_i \end{aligned} \quad (3)$$

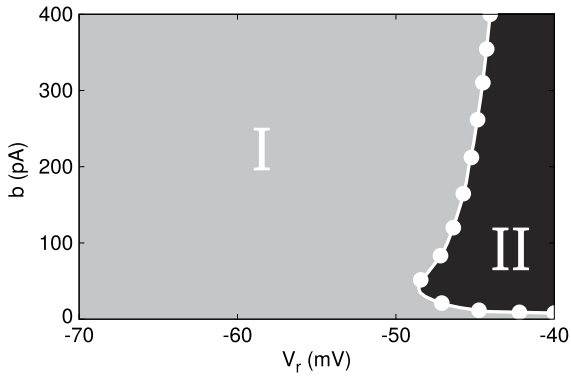


Fig. 2. Parameter space for the firing patterns as a function of the reset parameters V_r and b . Spike pattern in region I ($CV < 0.5$) and bursting pattern in region II ($CV \geq 0.5$) are separated by white circles.

where V_i is the membrane potential of the neuron i , g_s is the synaptic conductance, V_{REV} is the synaptic reversal potential, τ_s is the synaptic time constant, s_i is the synaptic weight, A_{ij} is the adjacency matrix, I_i is the external perturbation, and a_i is randomly distributed in the interval $[1.9, 2.1]$ to simulate a network composed by neurons with different parameters. We consider $I_i = 509.7$ pA, $V_{REV} = 0$ mV (excitatory) or $V_{REV} = -80$ mV (inhibitory), $\tau_s = 2.728$ ms, and $N = 100$. For this I_i value, when the neurons are uncoupled ($g_s = 0$), they spike with a frequency of about 9.2 Hz. In addition, I_i is a control parameter that can avoid large firing rate. The synaptic conductance g_s represent the strength of the excitatory (g_{ex}) or inhibitory (g_{in}) connections. The time-step of integration is 10^{-2} .

We consider a neuronal network model where each neuron is randomly linked to other neurons with a probability p by means of directed connections. When p is equal to 1, the neuronal network becomes an all-to-all network. A network with this topology was used by [Borges et al. \(2016\)](#) to study the effects of the spike timing-dependent plasticity on the synchronisation in a Hodgkin–Huxley neuronal network.

A useful diagnostic tool to determine synchronous behaviour is the complex phase order parameter defined as ([Kuramoto, 2003](#))

$$z(t) = R(t) \exp(i\Phi(t)) \equiv \frac{1}{N} \sum_{j=1}^N \exp(i\psi_j), \quad (4)$$

where R and Φ are the amplitude and angle of a centroid phase vector, respectively, and the phase is given by

$$\psi_j(t) = 2\pi m + 2\pi \frac{t - t_{j,m}}{t_{j,m+1} - t_{j,m}}, \quad (5)$$

where $t_{j,m}$ corresponds to the time when a spike m ($m = 0, 1, 2, \dots$) of a neuron j happens ($t_{j,m} < t < t_{j,m+1}$). We have considered the beginning of the spike when $V_j > -20$ mV. The value of the order parameter magnitude goes to 1 in a totally synchronised state. To study the neuronal synchronisation of the network, we have calculated the time-average order-parameter, that is given by

$$\bar{R} = \frac{1}{t_{fin} - t_{ini}} \sum_{t_{ini}}^{t_{fin}} R(t), \quad (6)$$

where $t_{fin} - t_{ini}$ is the time window for calculating \bar{R} . We consider a time window equal to 10^4 ms and one trial to compute \bar{R} due to the fact that the results do not have any qualitative dependence on the initial conditions.

[Fig. 3\(a\)–\(c\)](#) show the raster plots of the excitatory neuronal network for $g_{ex} = 0.02$ nS, $g_{ex} = 0.19$ nS, and $g_{ex} = 0.45$ nS,

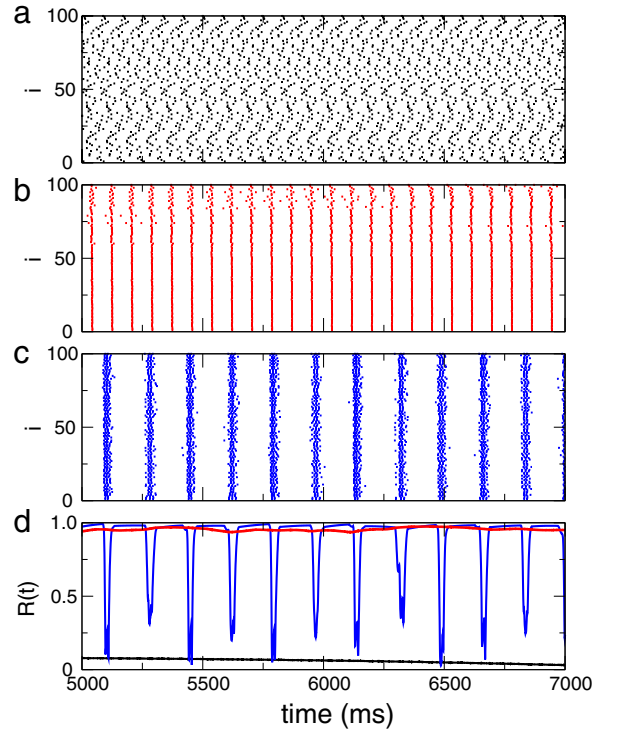


Fig. 3. (Colour online) Raster plot of the excitatory neuronal network for (a) $g_{ex} = 0.02$ nS, (b) $g_{ex} = 0.19$ nS, and (c) $g_{ex} = 0.45$ nS, considering $V_r = -58$ mV, $p = 0.5$, and $b = 70$ pA. In (d) the order parameter is computed for $g_{ex} = 0.02$ nS (black line), $g_{ex} = 0.19$ nS (red line), and $g_{ex} = 0.45$ nS (blue line).

respectively, considering $V_r = -58$ mV, $p = 0.5$, and $b = 70$ pA, where the dots correspond to the spiking activities generated by neurons. For $g_{ex} = 0.02$ nS ([Fig. 3\(a\)](#)) the network displays a desynchronised state, and as a result, the order parameter values are very small (black line in [Fig. 3\(d\)](#)). Increasing the synaptic conductance for $g_{ex} = 0.19$ nS, the neuronal network exhibits spike synchronisation ([Fig. 3\(b\)](#)) and the order parameter values are near unity (red line in [Fig. 3\(d\)](#)). When the network presents bursting synchronisation ([Fig. 3\(c\)](#)), the order parameter values vary between $R \approx 1$ and $R \ll 1$ (blue line in [Fig. 3\(d\)](#)). $R \ll 1$ to the time when the neuron is firing.

In [Fig. 4\(a\)](#) we show \bar{R} as a function of g_{ex} of the excitatory neuronal network for $p = 0.5$, $b = 50$ pA (black line), $b = 60$ pA (red line), and $b = 70$ pA (blue line). The three results exhibit strong synchronous behaviour ($\bar{R} > 0.9$) for many values of g_{ex} when $g_{ex} \gtrsim 0.4$ nS. However, for $g_{ex} \lesssim 0.4$ nS, it is possible to see synchronous behaviour only for $b = 70$ pA in the range 0.15 nS $< g_{ex} < 0.25$ nS. The curves have a bimodal nature, the minimal point happening due to the fact of the transition between spiking and bursting synchronisation occurs by means of a process of desynchronisation. In addition, we calculate the coefficient of variation (CV) to determine the range in g_{ex} where the neurons of the network have spiking or bursting behaviour ([Fig. 4\(b\)](#)). We consider that for $CV < 0.5$ (black dashed line) the neurons exhibit spiking behaviour, while for $CV \geq 0.5$ the neurons present bursting behaviour. We observe that in the range 0.15 nS $< g_{ex} < 0.25$ nS for $b = 70$ pA there are spiking synchronisation, and bursting synchronisation for $g_{ex} \gtrsim 0.4$ nS.

When g_{ex} is small, our neuronal network is like weakly coupled oscillators (WCO). The theory of WCO can be utilised not only to predict phase locking, but also to reduce the dynamics to a set of phase equations ([Hoppensteadt & Izhikevich, 1997](#)). [Hansel, Mato, and Meunier \(1993\)](#) studied Hodgkin–Huxley neurons coupled by weak excitatory interactions. They showed that excitatory

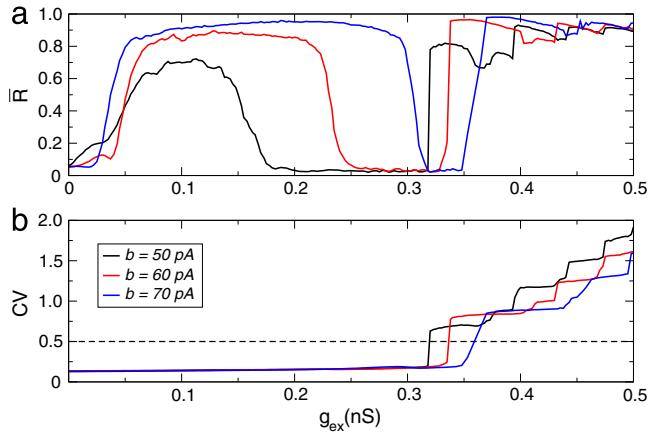


Fig. 4. (Colour online) (a) Time-average order parameter and (b) CV of the excitatory neuronal network for $V_r = -58$ mV, $p = 0.5$, $b = 50$ pA (black line), $b = 60$ pA (red line), and $b = 70$ pA (blue line).

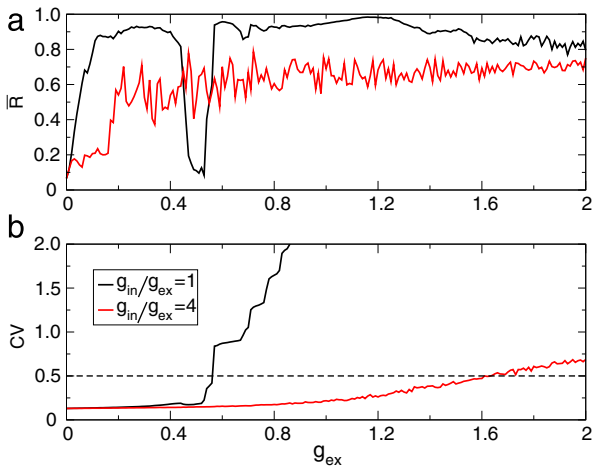


Fig. 5. (Colour online) (a) Time-average order parameter and (b) CV of the excitatory–inhibitory neuronal network for $V_r = -58$ mV, $p = 0.5$, $b = 70$ pA, $V_r = -58$ mV, and $I_i = 509.7$ pA, where we consider $g_{in}/g_{ex} = 1$ (black line) and $g_{in}/g_{ex} = 4$ (red line).

coupling may have significant consequences in the firing rates between the neurons. In fact, we observe that when aEIF neurons are weakly connected ($g_{ex} < 0.1$) by excitatory connections, neurons present significant levels of spiking synchronisation.

Ostojic (2014) studied asynchronous activity in balanced networks of excitatory and inhibitory neurons in integrate-and-fire (LIF). We study the influence of the contribution of the relative inhibitory and excitatory strength on the firing patterns. Fig. 5(a) and (b) exhibit \bar{R} and CV, respectively, for the neuronal network with 80% of excitatory and 20% of inhibitory connections. Comparing the results of Fig. 5 for $g_{in}/g_{ex} = 1$ with Fig. 4 (blue line), we find similar behaviour in both cases, namely spiking and bursting synchronisation with a transition region. However, when $g_{in}/g_{ex} = 4$ the overall synchronous level, measured by the order parameter (Fig. 5(a)), decreases. Moreover we verify desynchronised spikes for $0 < g_{ex} \lesssim 1.6$, as well as desynchronised spikes and bursts for $g_{ex} \gtrsim 1.6$ (Fig. 5(b)). The increase of the relative inhibition strength suppresses the synchronisation.

4. Parameter space of synchronisation

The synchronous behaviour depends on the synaptic conductance and the probability of connections. In this section, we analyse the parameter space of synchronisation of the excitatory

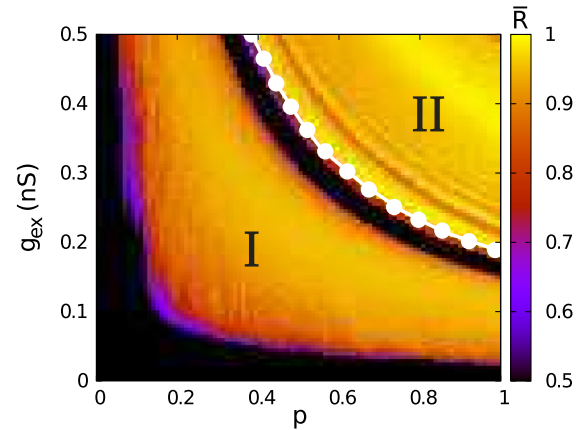


Fig. 6. (Colour online) Excitatory synaptic conductance g_{ex} as a function of the probability p for $V_r = -58$ mV and $b = 70$ pA, where the colour bar represents the time-average order parameter. The regions I (spike patterns) and II (bursting patterns) are separated by the white line with circles.

neuronal network. Fig. 6 exhibits the time-averaged order parameter in colour scale as a function of g_{ex} and p . We verify a large parameter region where spiking and bursting synchronisation is strong, characterised by $\bar{R} > 0.9$. The regions I and II correspond to spiking and bursting patterns, respectively, and these regions are separated by a white line with circles. We obtain the regions by means of the coefficient of variation (CV). There is a transition between region I and region II, where neurons initially synchronous in the spike, loose spiking synchronicity to give place to a neuronal network with a regime of bursting synchronisation.

We investigate the dependence of spiking and bursting synchronisation on the control parameters b and V_r . To do that, we use the time average order parameter and the coefficient of variation. Fig. 7 shows that the spike patterns region (region I) decreases when g_{ex} increases. This way, the region I for $b < 100$ pA and $V_r = -49$ mV of parameters leading to no synchronous behaviour (Fig. 7(a)), becomes a region of parameters that promote synchronised bursting (Fig. 7(b) and (c)). However, a large region of desynchronised bursting appears for $g_{ex} = 0.25$ nS about $V_r = -45$ mV and $b > 100$ pA in the region II (Fig. 7(b)). For $g_{ex} = 0.5$ nS, we see, in Fig. 7(c), three regions of desynchronous behaviour, one in the region I for $b < 100$ pA, other in region II for $b < 200$ pA, and another one is located around the border (white line with circles) between regions I and II for $b > 200$ pA.

Fig. 7 shows multiple regions of asynchronous behaviour in II. In this region, we observe the existence of not only bursting behaviour happening for long time intervals, but also happening for short time intervals such as shown in Fig. 8(a). Fig. 8(a) and (b) exhibit the action potential and the raster plot, respectively, for parameters in the region II shown in Fig. 7(a) with a white triangle. In general, $CV > 0.5$ characterises a network with neurons presenting irregular spikes. More specifically, we have verified in our neuronal network model that $CV > 0.5$ characterises a network with a bursting pattern. The signal, shown in Fig. 8, \bar{R} is equal to 0.54 and CV is equal to 2.96.

It has been found that external perturbations on neuronal networks not only can induce synchronous behaviour (Baptista, Zhou, & Kurths, 2006; Zhang, Li, Huang, & Xiao, 2015), but also can suppress synchronisation (Lameu et al., 2016). Aiming to study the robustness to perturbations of the synchronous behaviour, we consider an external perturbation I_i in Eq. (3) described by a uniform discrete random process which takes values at each integration step within the interval $[0, 1]$. It is applied on each neuron i with an average time interval of about 10 ms and with a constant intensity γ during 1ms. We also study how this external perturbation disturbs a neuronal network. We initially

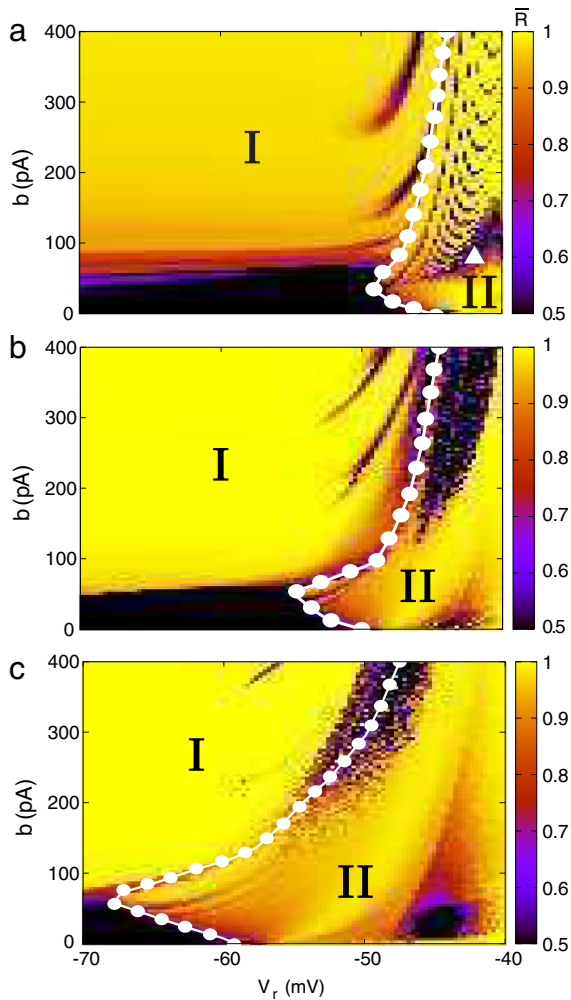


Fig. 7. (Colour online) Parameter space $b \times V_r$ for $p = 0.5$, $\gamma = 0$ (a) $g_{ex} = 0.05$ nS, (b) $g_{ex} = 0.25$ nS, and (c) $g_{ex} = 0.5$ nS, where the colour bar represents the time-average order parameter. The regions I (spike patterns) and II (bursting patterns) are separated by white circles. The white triangle corresponds to $b = 86$ pA and $V_r = -43$ mV.

set an unperturbed neuronal network for parameters that leads to synchronous behaviour. When synchronisation is achieved, we turn the external perturbation on.

Fig. 9 shows the plots $g_{ex} \times p$ for $\gamma > 0$, where the regions I and II correspond to spiking and bursting patterns, respectively, separated by white line with circles, and the colour bar indicates the time-average order parameter values. In this figure, we consider $V_r = -58$ mV, $b = 70$ pA, (a) $\gamma = 250$ pA, (b) $\gamma = 500$ pA, and (c) $\gamma = 1000$ pA. For $\gamma = 250$ pA (Fig. 9(a)) the perturbation does not suppress spike synchronisation, whereas for $\gamma = 500$ pA the synchronisation is completely suppressed in region I (Fig. 9(b)). In Fig. 9(c), we see that increasing further the constant intensity for $\gamma = 1000$ pA, the external perturbation suppresses also bursting synchronisation in region II. Therefore, the synchronous behaviour in region II is more robust to perturbations than in the region I, due to the fact that the region II is in a range with high g_{ex} and p values, namely strong coupling and high connectivity.

In order to understand the perturbation effect on the spike and bursting patterns, we consider the same values of g_{ex} and p as Fig. 7(a). Fig. 10 exhibits the space parameter $b \times V_r$, where γ is equal to 500 pA. The external perturbation suppresses synchronisation in the region I, whereas we observe synchronisation in region II. The synchronous behaviour in region II can be suppressed if the constant intensity γ is increased. Therefore, bursting

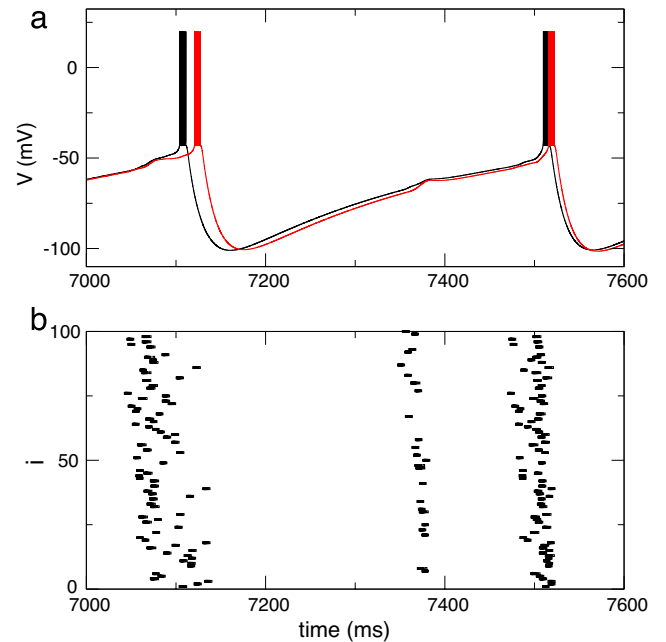


Fig. 8. (Colour online) (a) Action potential for two neurons and (b) raster plot for $p = 0.5$, $b = 86$ pA, $V_r = -43$ mV, $g_{ex} = 0.05$ nS, and $I_i = 509.7$ pA.

synchronisation is more robust to perturbations than spike synchronisation.

5. Conclusion

In this paper, we studied the spiking and bursting synchronous behaviour in a random neuronal network where the local dynamics of the neurons is given by the adaptive exponential integrate-and-fire (aEIF) model. The aEIF model can exhibit different firing patterns, such as adaptation, tonic spiking, initial burst, regular bursting, and irregular bursting.

In our network, the neurons are randomly connected according to a probability. The larger the probability of connection, and the strength of the synaptic connection, the more likely is to find bursting synchronisation.

It is possible to suppress synchronous behaviour by means of an external perturbation. However, synchronous behaviour with higher values of g_{ex} and p , which typically promotes bursting synchronisation, are more robust to perturbations, than spike synchronisation appearing for smaller values of these parameters. Moreover, we have verified that bursting synchronisation is more robust not only to larger γ values, but also for different external perturbation frequencies. The synchronised region in $g_{ex} \times p$ depends on the external perturbation amplitude and frequency. We concluded that bursting synchronisation provides a good environment to transmit information when neurons are strongly perturbed (large Γ).

The neurons desynchronise near the border between regions I to II. The dynamical fundamentals for this transition to occur are still unclear to us and require further investigation. However, giving the alignment of the border along the vertical coordinates b , this phenomenon is critically dependent on the resetting potential V_r in that for larger values it induces bursting behaviour.

Acknowledgements

This study was possible by partial financial support from the following Brazilian government agencies: CNPq (433782/2016-1), CAPES, and FAPESP (2011/19296-1, 2015/07311-7 and 2016/16148-5). We also wish to thank Newton Fund and COFAP.

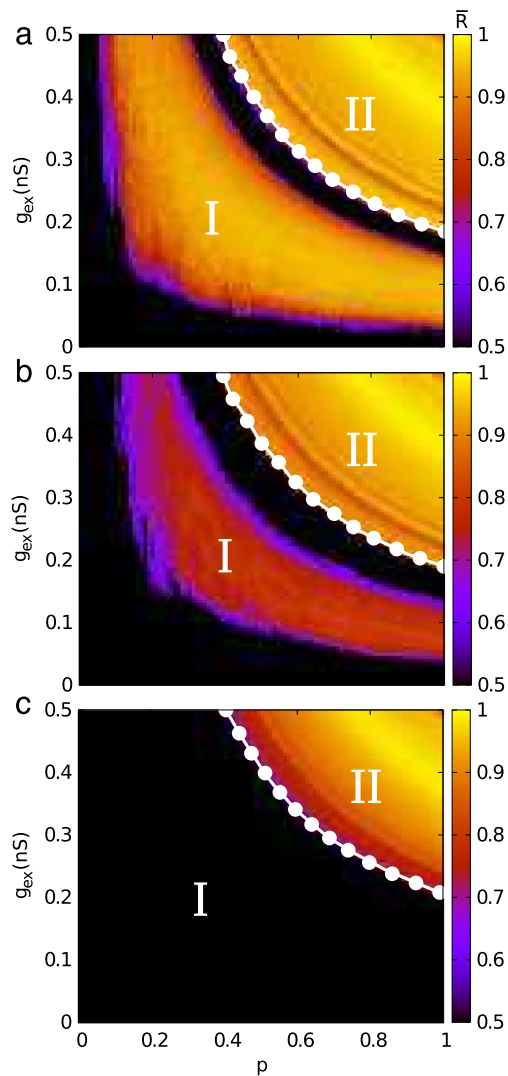


Fig. 9. (Colour online) Excitatory synaptic conductance g_{ex} as a function of the probability p for $V_r = -58$ mV, $b = 70$ pA, (a) $\gamma = 250$ pA, (b) $\gamma = 500$ pA, and (c) $\gamma = 1000$ pA.

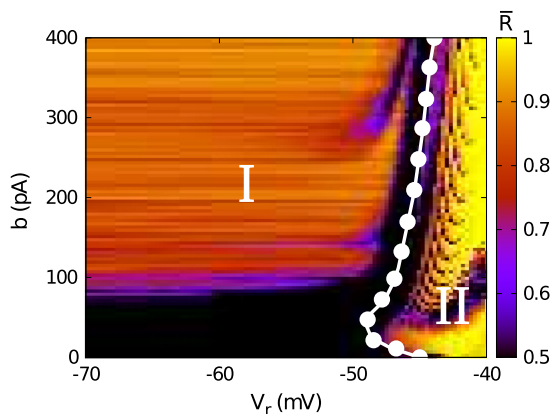


Fig. 10. (Colour online) Parameter space $b \times V_r$ for $g_{\text{ex}} = 0.05$ nS, $p = 0.5$, and $\gamma = 500$ pA, where the colour bar represents the time-average order parameter. The regions I (spike patterns) and II (bursting patterns) are separated by white line with circles.

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