

Background subtraction and normalization in SANS and SAXS

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Schematic setup for small-angle scattering

Sample: Dilute solutions with 1% concentration



Sample



Dilute solution (1% = 10 mg/mL) of particles

 random orientation of particles
 centro symmetric intensity distribution on detector

Scattering vector q

 $q \equiv 4\pi \sin \theta / \lambda$

Bragg's Law:

$$q = n \frac{2\pi}{d}$$



Data Treatment Particles in Solution



Input data: Azimuthally averaged data

 $q_i, I(q_i), \sigma[I(q_i)] \quad i = 1, 2, 3, ... N$

 q_i calibrated

- $I(q_i)$ calibrated, i.e. on absolute scale - noisy, (smeared), truncated
- $\sigma[I(q_i)]$ Statistical standard errors: Calculated from counting statistics by error propagation - do not contain information on systematic error !!!!

Intensity and Differential Scattering Cross Section

$$I(q) = \frac{d\sigma}{d\Omega}(q)$$

number of scattered neutrons or photons per unit time, relative to the incident flux of neutron or photons, per unit solid angle at q per unit volume of the sample.

Unit : cm^{-1}

Absolute scale: SAXS

The absolute scattering of water can be calculated from the fundamental properties to be $I_{H2O}^{theory} = 0.0162 \text{ cm}^{-1}$.

$$I_{H2O} = nb^2 k_B T \chi_T$$

- *n*: number density of molecules
- *b*: scattering length of molecules
- k_BT : thermal energy
- χ_T : Isothermal compressibility

Convert to absolute scale using

$$I_{abs}(q) = I(q) \frac{I_{H2O}^{theory}}{I_{H2O}^{exp}}$$

The same for static light scattering but toluene is usually used

neutron and hydrogen parallel spins scatter very different from anti-parallel spins !

Random distribution -> incoherent scattering

$$I_{H2O}^{'theory'} = (1-T)/4\pi \ g(\lambda)$$

 $g(\lambda)$ is an empirical factor -varies with instrument and detector -include corrections for inelactic effects anf multiple scattering

$$I_{abs}(q) = I(q) \frac{I_{H2O}^{theory}}{I_{H2O}^{exp}}$$

SAXS data processing

- 1. SAXS NT (Bruker AXS) flood correction spatial correction azimuthal averaging (beamcenter) (distance calibration Ag-behenate)
- 2. Home-written software (SUPERSAXS package) conversion, inclusion of meta data plot background subtraction normalization (H2O) rebinning scaling...

Multi-wire position sensitive detector



•High quantum efficinecy

•0.5 mm (FWHM resolution)

•Saturation: 100'000 cps



Multi-wire position sensitive detector



Bruker AXS' HiSTAR detector



Gabriel type detector sold by Molecular Metrology Photons converted to charge particles and electrons followed by gas amplification



Limit: about 100 000 cps

Flood correction:

Use radioactive source ⁵⁵Fe decays to Mg and emits 5.8 keV x-rays (Cu Ka 8.0 keV!)



x and y projections used for correct to to uniform sensitivity

Spatial correction

Use plate with regularly spaced holes together with ⁵⁵Fe source



Spatial correction



Use plate with regularly spaced holes together with ⁵⁵Fe source

Local 'rubber' mask used for stretchin/compressing scales to map on uniform spacing

Distance calibration with Ag behenate (known lattice spacing!)



Azimuthal integration (beamcenter !)



Center Misalignment

q

SAXS: Small Angle X-ray Scattering System V4 1.30 Copyright 1997-2008 Broker AXS. Phylect. File. Edit. Collect. Process Analysis. Proba. Special. User. Help.	All oghts reserved.	리미치
unfor Teo Fie Deero Touries Bucker , offic Norses Teo Rich	40kV 30mA at 65cm	
	LDL_1_1.gfrm 09/03/10 16:24:26 Created 08/26/10 Mag,Quad 1 0 omega 0.00000 Width 0.2500 Counts 945566 Time (s) 7200.00 Distance 65.6800 Size 1024	2756
	Frame was taken at 2-Theta 0.00000 Omega 0.00000 Phi 0.00000 Chi 0.00000	736 380
		102
		52
		27
		14
		7
		4
	Distance 65.7500	2
	Spatial 1024_065 MA 30 1024x1024 No PDC	1

Only 3 pixels off !



Center Corrected !





Raw format: comment lines, then: theta, I, sig(I),q

```
!@!!GADDS PLOTSO FILE: Chi integration type
!@!!Title: 45kV 90mA at 64cm
!@!!Frame: $frame
                  1.54184
                             1.54056
                                      1.54439
!@!!Wavelengths
!@!!Integration range: 2Theta: 0.100 to 4.800 Gamma: -180.000 to 180.000
!@!!Integration method: bin normalized
!@!N
!@!SS
!@!M
!@!L 0.0 0.0 0.0 0.0
!@!XDegrees
!@!YCounts
                                       Theta,I,sig(I),q
0.10 38.333706 1.547870 0.007112
0.12 100.568771 2.288812 0.008535
0.14 182.932983 2.857968 0.009957
0.16 233.431747 3.019857 0.011380
0.18 242.650208 2.902801 0.012802
0.20 234.392487 2.706550 0.014225
0.22 224.673691 2.526560 0.015647
0.24 218.917648 2.387832 0.017070
0.26 210.772476 2.251053 0.018492
0.28 204.949387 2.138994 0.019915
0.30 202.736664 2.055254 0.021337
0.32 194.081619 1.947061 0.022760
0.34 189.383942 1.865945 0.024182
```

RAD format (.rad)

q,I,sig(I),theta,

I_PE (cps)	TIME	TRANSM	D(thickness) (mm)
6752.00	6000.00	0.105800	1.80
236			
0.711200E-	02 38.3337	1.54787	0.100000
0.853500E-	02 100.569	2.28881	0.120000
0.995700E-	02 182.933	2.85797	0.140000
0.113800E-	01 233.432	3.01986	0.160000
0.128020E-	01 242.650	2.90280	0.180000
0.142250E-	01 234.392	2.70655	0.200000
0.156470E-	01 224.674	2.52656	0.220000
0.170700E-	01 218.918	2.38783	0.240000
0.184920E-	01 210.772	2.25105	0.260000
0.199150E-	01 204.949	2.13899	0.280000
0.213370E-	01 202.737	2.05525	0.300000
0.227600E-	01 194.082	1.94706	0.320000
0.241820E-	01 189.384	1.86594	0.340000
0.256050E-	01 186.338	1.79872	0.360000
0.270270E-	01 177.610	1.70925	0.380000
0.284500E-	01 174.150	1.64965	0.400000
0.298720E-	01 167.297	1.57790	0.420000
0.312950E-	01 152.965	1.47412	0.440000
0.327170E-	01 144.600	1.40174	0.460000

RAD format (.rad)

q,I,sig(I),theta,

TIME

6000.00 236

.30			
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0.327170E-01	144.600	1.40174	0.460000

Measured intensity

 $I(q) \propto \frac{d\sigma}{d\Omega}(q) dAT \langle \Phi \rangle t \epsilon \Delta \Omega$

counts !

d: sample thickness *A*: beam cross section area *T*: sample transmission $\langle \Phi \rangle$: average flux (photons per second) *t*: measuring time ε : detector efficiency $\Delta \Omega$: solid angle of pixel

 $I_{abs}(q) = I(q) \frac{I_{H2O}^{max}}{I_{H2O}^{exp}}$

When using same capillary for sample and water measurement: d, A, ε , and $\Delta\Omega$ cancel

Note $\sigma(I(q)) = \sqrt{I(q)}$

Sample holder – home-build





Quartz capillary about 1.7 mm in diameter wall thickness of only 0.010 mm 50 μL is enough!

Capillary, quartz : 2 mm (actually 1.7 mm)



Sources of background

Solvent

Capillary

Instrument background (parasitic scattering, fluorescence, ...)

Detector noise

Normalization procedures

Normalize by $T\langle \Phi \rangle t$ ('Old' procedure for blocking beamstop)



Beamstop, semi-transparent 3 mm ø



Home-build

- Semitransparent with Ni filter
- T = 1/50000
- 5-20 cps behind beamstop
- Monitor on detector
- Intensity behind beamstop prop. to transmission and integrated flux

$$I_{BS} = k T \langle \Phi \rangle t$$

Raw data: linear scales



Logarithmic intensity scale



Measurements required

Measure:

sample in cell, $I_{\rm m}^{\rm sample}(q)$, solvent in cell, $I_{\rm m}^{\rm solvent}(q)$, noise with lead at sample position $I_{\rm m}^{\rm noise}(q)$,

H₂O in cell, $I_{\rm m}^{\rm H2O}(q)$, empty cell, $I_{\rm m}^{\rm cell}(q)$, noise with lead at sample position $I_{\rm m}^{\rm noise}(q)$.

Normalize by integrated intensity behind beamstop.....

Data Subtraction and Normalization

Measure sample, solvent, background, H₂O, empty cell using same cell:

(1)
$$I_{\rm m}^{\rm sample}(q) = k T_s \Phi_s t_s I_0^{\rm sample}(q) + k T_s \Phi_s t_s I_0^{\rm solvent}(q) + t_s I_0^{\rm noise}(q)$$

(2)
$$I_{\rm m}^{\rm solvent}(q) = k T_{sol} \Phi_{sol} t_{sol} I_0^{\rm solvent}(q) + t_{sol} I_0^{\rm noise}(q)$$

(3)
$$I_{\rm m}^{\rm noise}(q) = t_{noise} I_0^{\rm noise}(q)$$

(1)
$$k T_s \Phi_s t_s I_0^{\text{sample}}(q) = I_m^{\text{sample}}(q) - k T_s \Phi_s t_s I_0^{\text{solvent}}(q) - t_s I_0^{\text{noise}}(q)$$

(1)
$$I_0^{\text{sample}}(q) = I_m^{\text{sample}}(q)/(k T_s \Phi_s t_s) - I_0^{\text{solvent}}(q) - t_s I_0^{\text{noise}}(q)/(k T_s \Phi_s t_s)$$

(2)
$$k T_{sol} \Phi_{sol} t_{sol} I_0^{\text{solvent}}(q) = I_m^{\text{solvent}}(q) - t_{sol} I_0^{\text{noise}}(q)$$

(2)
$$I_0^{\text{solvent}}(q) = I_m^{\text{solvent}}(q)/(k T_{sol} \Phi_{sol} t_{sol}) - t_{sol} I_0^{\text{noise}}(q)/(k T_{sol} \Phi_{sol} t_{sol})$$

(3)
$$I_0^{\text{noise}}(q) = I_m^{\text{noise}}(q) / t_{noise}$$

Data Subtraction and Normalization

(1)+(2):
$$I_0^{\text{sample}}(q) = I_m^{\text{sample}}(q)/(k T_s \Phi_s t_s)$$

$$- [I_m^{\text{solvent}}(q)/(k T_{sol} \Phi_{sol} t_{sol}) - t_{sol} I_0^{\text{noise}}(q)/(k T_{sol} \Phi_{sol} t_{sol})]$$

$$- t_s I_0^{\text{noise}}(q)/(k T_s \Phi_s t_s)$$

use also (3):
$$I_0^{\text{sample}}(q) = I_m^{\text{sample}}(q)/(k T_s \Phi_s t_s)$$

 $- [I_m^{\text{solvent}}(q)/(k T_{sol} \Phi_{sol} t_{sol}))$
 $- t_{sol} \{I_m^{\text{noise}}(q)/t_{noise}\}/(k T_{sol} \Phi_{sol} t_{sol})]$
 $- t_s \{I_m^{\text{noise}}(q)/t_{noise}\}/(k T_s \Phi_s t_s)$

$$= I_n^{\text{sample}}(q) - I_n^{\text{solvent}}(q)$$

+ $t_{sol} I_n^{\text{noise}}(q) / (k T_{sol} \Phi_{sol} t_{sol})$
- $t_s I_n^{\text{noise}}(q) / (k T_s \Phi_s t_s)$

$$= I_n^{\text{sample}}(q) - I_n^{\text{solvent}}(q) - I_n^{\text{noise}}(q) [t_s / (k T_s \Phi_s t_s) - t_{sol} / (k T_{sol} \Phi_{sol} t_{sol})]$$

Data Subtraction and Normalization

Error calculation!!!!

The same is done for water and empy cell measurements !

Raw water data, no normalization



Raw water data, normalization by transmission and time Water and background



Water and background

Water with extrapolation

Water, background subtrackted



Shaddowing by beamstop



Shaddowing by beamstop at detector



Note: Difference in BS center and q scale zero point also gives Smearing of BS edge!!!

Correction

BS(q) Beamstop response function (step) D(q) Detector resonse function (Gaussian, FWHM=0.5 mm) I(q) Scattering from sample, more slowly varying than BS(q) and D(q)

$$I_{meas}(q) = \int D(q-q')BS(q')I(q')dq'$$

When I(q) slowly varying: $I_{meas}(q) \approx I(q) \int D(q-q')BS(q')dq'$

So that:
$$I(q) \approx I_{meas}(q) / \int D(q-q')BS(q')dq'$$

Note: For difference in BS center and q scale zero point, this correction is strickly correct!

How do we measure $\int D(q-q')BS(q')dq'$?

GC correction



GC correction





The correction is striktly valid for this effect!

Calculated examples

No misalignment!

R_BS=1.4 mm, sampl-det=660 mm, q_min=0.009 1/Å Det_FWHM=0.4 mm, Gaussian detector resolution function Solid spheres

q	R=50Å	R=50Å	R=100Å	R=100Å	R=200Å	R=200Å	R=300 Å l	R=300Å	R=400 Å	R=400Å
(1/Å)	corr	uncorr	corr	uncorr	corr	uncorr	corr	uncorr	corr	uncorr
0.007	2%	97%	8%	97%	29%	98%	60%	99%		100%
0.008	1	83	5	84	22	87	49	91	83	97
0.009	0	50	3	50	13	57	34	67	71	86
0.010	0	17	1	17	6	22	18	32	52	60
0.011	0	3	0	3	1	4	6	8	25	27
0.012	0	0	0	0	0	0	3	3	3	3
0.013	0	0	0	0	0	0	0	0	0	0

For Det_FWHM=0.15 mm, all data for q=0.010 1/Å and larger can be used for all sizes !!!!

It is very important to improve detector resolution to improve realiability of data close to q_min !!!!!

An example P85 Pluronic: EO 23-PO 40-EO 23



An example P85 Pluronic: Log-Log plot







An example P85 Pluronic: Log rebinning



Summary

- Principles of
 - •calibration
 - background subtraction
 - •Absolute normalization
- Now to SuperSAXS program package

$S_U_P_E_R_S_A_X_S$

PROGRAM PACKAGE FOR DATA TREATMENT, ANALYSIS AND MODELING



Cristiano L P Oliveira

Jan Skov Pedersen

Package characteristics

- Made in FORTRANTM language
- Uses GNUPLOTTM Graphics interface
 - Compilable in any operating system
- Build in modular blocks
 - Easy to update, improve and integrate
- User friendly

File Formats

- **<u>RAW files</u>**-> Angular Integrated Data from the aquisition program
- **RAD files**-> RAW data converted to JSP format
- **RDN files**-> Beam stopper shadow correction file
- **RDS files**-> Background subtracted Data
- **RSR files**-> Rebinned data
- SCA files-> Scaled Data
- **LIS files**-> List of files for many applications

MS-DOS Prompt - PROGS	
C:\crislpo\AARHUS~1\Lecture\TREATM~1\RDS-RSR>PROGS	

S_U_P_E_R_S_A_X_S PROGRAMS	
***************************************	-
List of Available Programs :	
LIST.EXE -> Creates file lists for other programs	_
WAOG, EXE -> Averages KAD KDS KSK files giving chi2	
WCOMP.EXE -> Compares and rescales two input files	
WUNDLEXE -> Converts data file to JSP format files	
WIFILERE -> Perform inverse fourier transformation	
WGNOFLOI.EXE-/ Gnuplot rogram (www.gnuplot.info/	
WGROWNLEAE -/ Greates a normalization file for heam	
Stopper Shadow Correction	
MUDIOT FYE -> Diote . ISP format files Reade a list	
WREDILLE - Proto bol formatifuically seling	
of input files Reads TARAD FIL file	
$WSXH20$ FXF \rightarrow Data treatment for water files and	
zero intensitu fit	
WSXSUB.EXE \rightarrow Data treatment for SAXS data files	
and normalization to absolute scale	
WTORAD.EXE -> Converts RAW files to RAD files.	
Reads TORAD.FIL file.	
If the prompt not appear, press Ctrl+C	_
	-

List directed procedure





Data Treatment of SAXS Data

$$I_{Treated}(q) = \left[\left(\frac{I_{sample}(q)}{\Phi_s.T_s.t_s} - \frac{I_{back}(q)}{\Phi_b.T_b.t_b} - \frac{I_{noise}(q)}{t_{noise}(\Phi_s.T_s - \Phi_b.T_b)} \right) \frac{1}{I_{shadow}(q)} \right] \frac{d\Sigma / d\Omega_{water, 20^{\circ}C}}{I(0)_{water, 20^{\circ}C}}$$

$$\sigma_{treated}(q) = \left(\frac{\sigma_1(q)^2}{I_{shadow}(q)^2} + \left(\frac{I_{sample}(q)}{\Phi_s.A_s.t_s}\right)^2 \frac{\sigma_{shadow}(q)^2}{I_{shadow}(q)^2}\right)^{1/2} \qquad \sigma_1(q) = \sigma_{sample}(q)^2 + \sigma_{hack}(q)^2 + \sigma_{noise}(q)^2 \left(\frac{1}{\Phi_s.A_s} - \frac{1}{\Phi_b.A_b}\right)^2$$

Bevington (1992), Data Reduction and Error Analysis for the Physical Sciences

- •*I(q)* is the measured (integrated) scattering intensities
- • $\boldsymbol{\Phi}$ is the intensity incident beam
- •*T* is the sample transmission
- *t* is the exposition time
- • $\sigma(q)$ is the statistical error of each point.

• $I_{shadow}(q)$, $\sigma_{shadow}(q)$ are the normalized intensity and error for the beam stopper shadow correction





MS-DOS Prompt	- 🗆 🗙
Buffer File : B2.RAD	
Output File	

Water file for absolute norm> WATERNM.PAR	
Used capillary #	
File 1 opened : Sample	
rite 2 upeneu - backgruunu	
File 3 opened : Dark Current> LEAD 06.RAD	
File 4 opened : Normalization File> 06APR_GC.RDN	
File 5 Opened : Output File> S2.RDS	
0.951 1 DIRECT RATIO 0.99996E-02 0.10517E-01	
0.959 2 DIRECI HREH-W RHIIU	
1 010 4 DIRECI AREA-W ANIIO	
1.037 5 DIRECT AREA-W RATIO	
0.987 SIMPLE RATIO OF AREAS 0.24506E+00 0.24819E+00	
Smallest Value of Intensity> 0.00000E+00	
Change Scale of Transmission (Y,N)?n	
Data Tugatment Rinished ***	
pata ireatment rinisneu ::: If the nyomet not annear nyess (ty)+C	
AC and broube use abboard broos out - 3	
C:\crislpo\AARHUS~1\DATA_0~1\OTZEN\TREATM~1>_	-

Data Rebinning



Rebinning of experimental data speeds up operations with the data and also decreases the noise.

Linear rebinning (points equally spaced in linear scale) of scattering data can generate artefacts on the scattering profile

Logarithmic rebinning (points equally spaced in log scale) of scattering decreases considerably the number of points, preserving the features of experimental data

It is not recommended for curves with sharp peaks







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Future Perspectives

• Increase the applicability of the package, adding more features

- Develop the program interface
- Correct Bugs!